



# Tier 3

## Intervention Lessons

7.NS.2c

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness for 8.EE.7b:** Solve multi-step linear equations

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# Tier 3 Intervention Planning Guide

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

<b>Recommended Actions</b>	
<b>Beginning</b> (5 min.)	<ul style="list-style-type: none"> <li>➤ Review the learning target with the whole group</li> <li>➤ Ask each student to set a goal for the day based on their previous Quick Check Score</li> <li>➤ Have each student use a highlighter to plot their goal for the day</li> </ul>
<b>Middle</b> (15 min.)	<ul style="list-style-type: none"> <li>➤ Model solving a word problem – “I do” (<i>Sessions 1, 3 and 6 only</i>)</li> <li>➤ Guided Practice – “We do”</li> </ul> <p><b>Sessions 1 and 2:</b> Multiply and divide using integer tiles</p> <p><b>Sessions 3, 4 and 5:</b> Multiply and divide using integer drawings</p> <p><b>Sessions 6, 7 and 8:</b> Multiply and divide using understanding of multiplication and division</p>
<b>End</b> (10 min.)	<ul style="list-style-type: none"> <li>➤ Bring the students back together</li> <li>➤ Ask students to reflect on their progress towards the learning target               <ul style="list-style-type: none"> <li>○ What did I learn today about multiplying and dividing by integers between -10 and 10?</li> <li>○ How confident do you feel about multiplying and dividing by integers between -10 and 10 on my own? (Thumbs up, down, or sideways)</li> </ul> </li> <li>➤ Assess each student’s progress using the next <b>Quick Check</b> form</li> <li>➤ Guide students to self-correct their <b>Quick Check</b></li> <li>➤ Guide students to chart their progress in their <b>Growth Chart</b> <ul style="list-style-type: none"> <li>○ If not using Delta Math lessons, record the activity in the table</li> </ul> </li> <li>➤ Collect each student’s <b>Quick Check</b> and <b>Growth Chart</b></li> </ul>
<b>After</b> <b>Session 6</b>	<ul style="list-style-type: none"> <li>➤ Differentiation Options:               <ul style="list-style-type: none"> <li>○ Allow students who met the learning goal to work independently while others do the guided practice during the next session</li> <li>○ Exit students who met the learning goal for a third time</li> </ul> </li> <li>➤ Problem solve with a team to plan additional support for students who do not meet the learning goal within 8 sessions</li> </ul>



# Session 1: Modeling (I Do)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

Sam's grandma keeps track of money that she loans him in a notebook called "Sam's Financial Journal". The recent balance was 0 dollars and his grandma gave him money to purchase three \$2 hotdogs. What is the current balance in the journal?

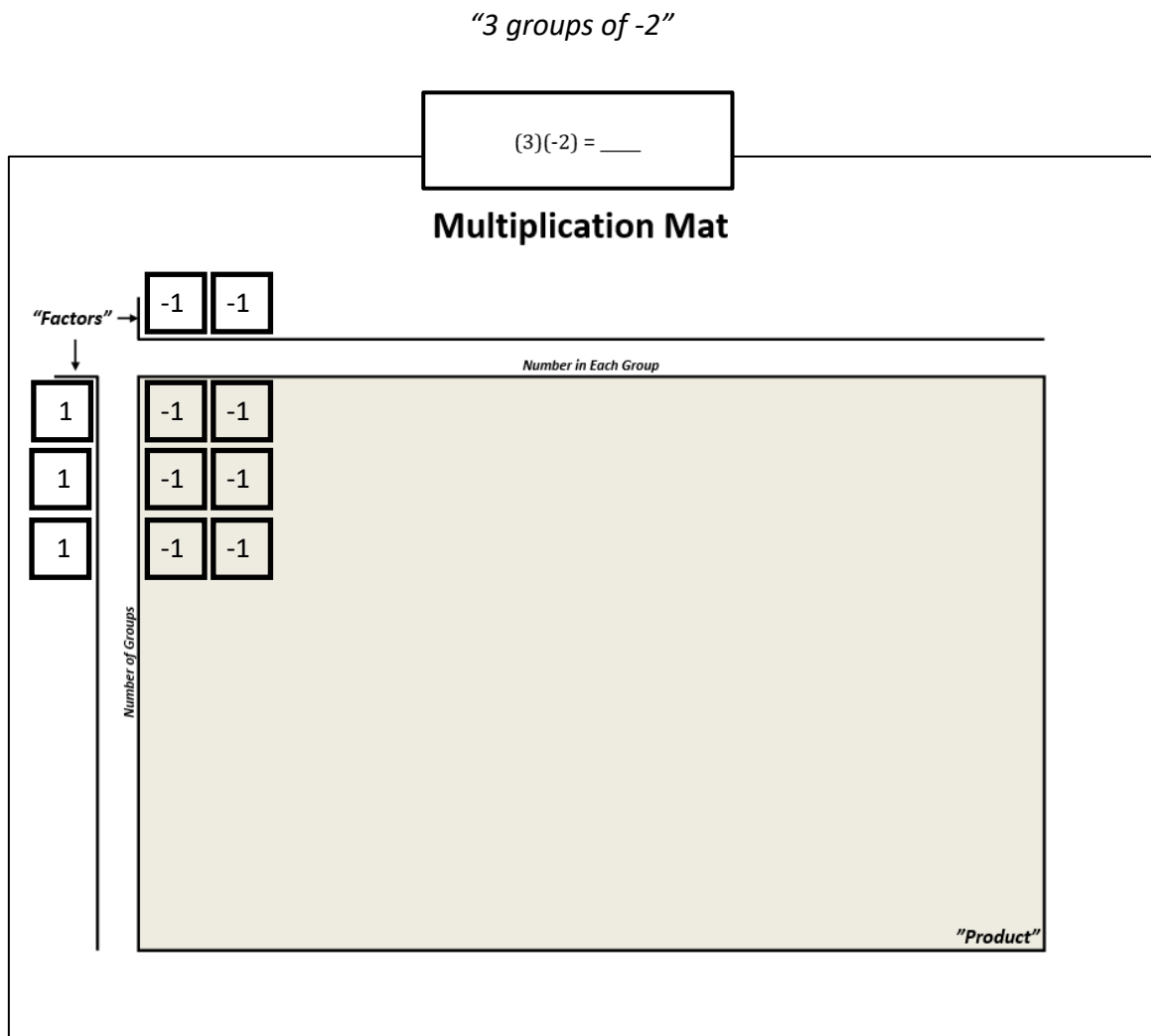


# Session 1: Modeling (*I Do – Visual Support*)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

Sam’s grandma keeps track of money that she loans him in a notebook called “Sam’s Financial Journal”. The recent balance was 0 dollars and his grandma gave him money to purchase three \$2 hotdogs. What is the current balance in the journal?





# Session 1: Modeling (I Do - Teacher Notes)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

Sam’s grandma keeps track of money that she loans him in a notebook called “Sam’s Financial Journal”. The recent balance was 0 dollars and his grandma gave him money to purchase three \$2 hotdogs. What is the current balance in the journal?

**I am going to think aloud to model solving this problem.**

**Your job is to watch, listen, think and ask questions.**

**First, it is important to know what the problem is about.**

**The problem is about “Sam’s Financial Journal”.**

**Second, I need to determine what I need to find.**

**I need to find the current balance.**

**Third, I need to determine what I know.**

**I know the recent balance was 0 dollars and his grandma gave him money to purchase three \$2 hotdogs. Also, I know money that is owed...or debt...can be represented as negative integers and money earned can be represented as positive integers.**

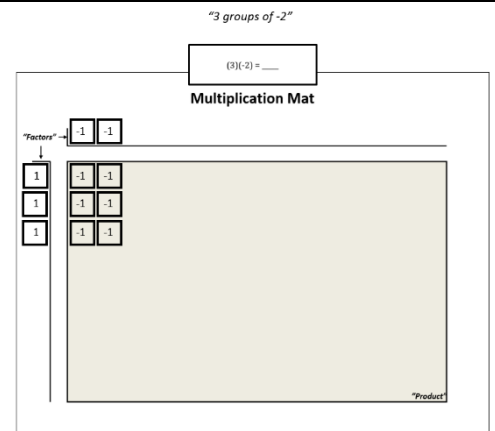
**Fourth, I need to figure out what I can try.**

**I am going to try using integer tiles and equation cards to find Sam’s current balance.**

**Since I need 3 groups of 2 negative chips to model Sam’s current debt... I can use the equation card 3 times -2 to model this situation.**  
*(Place 3 “+1 tiles” and 2 “-1 tiles” as the factors to the problem and the equation card near the top of the multiplication mat.)*

**Now, I will place 3 sets of 2 “-1 tiles” to show the current balance.**  
*(Place 3 sets of 2 “-1 tiles” on the mat.)*

**I see 2...4...6 negative 1 tiles...that represents -6 dollars...or 6 dollars of debt to pay.**  
*(Point to the 6 “-1 tiles” that make up the product.)*



**Last, I need to make sure that my answer makes sense.**

**I found that Sam’s balance is 6 dollars of debt. It makes sense because I modeled the situation using integer tiles as the factors. Then, I modeled the product with 2 groups of 3 “-1 tiles” to show 6 dollars of debt as the current balance in the journal.**



# Modeling & Guided Practice Cards

Use for Problem 1 $3(-5) = \underline{\quad}$	Use for Problem 2 $-12 \div 4 = \underline{\quad}$
Use for Problem 3 $4 \times -3 = \underline{\quad}$	Use for Problem 4 $-4(3) = \underline{\quad}$
Use for Problem 5 $2(-5) = \underline{\quad}$	Use for Problem 6 $-12 \div 3 = \underline{\quad}$
Use for Problem 7 $5 \times -3 = \underline{\quad}$	Use for Problem 8 $-2 \times 3 = \underline{\quad}$
Use for Problem 9 $-10 \div 2 = \underline{\quad}$	Use for Problem 10 $-16 \div -8 = \underline{\quad}$
Use for Modelling $3(-2) = \underline{\quad}$	

# Integer Tiles (3 Sets)

+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
+1	+1	+1	+1	+1	+1	+1	+1	+1	+1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1





Name \_\_\_\_\_

Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 1: Guided Practice (We Do)

**Materials:**

- Integer Tiles (20 positive and 20 negative tiles)
- Integer Equation Cards (1 set)

**Note:** If there is no addition or subtraction symbol between the first integer and the parentheses, then the integers should be multiplied.

$$2(-4) = 2 \times -4$$

$$-3(7) = -3 \times 7$$

$$-4(-5) = -4 \times -5$$

$$(-2)(6) = -2 \times 6$$

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use integer tiles to find the answer.

<p>1.</p> $3(-5) = \underline{\quad}$	<p>2.</p> $-12 \div 4 = \underline{\quad}$
<p>3.</p> $4 \times -3 = \underline{\quad}$	<p>4.</p> $-4(-3) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 1: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to multiply or divide using integer tiles.

5. $2(-5) = \underline{\quad}$	6. $-12 \div 3 = \underline{\quad}$
7. $5 \times -3 = \underline{\quad}$	8. $-2 \times 3 = \underline{\quad}$
9. $-10 \div 2 = \underline{\quad}$	10. $-16 \div -8 = \underline{\quad}$

**Learning Target:** I will multiply and divide by integers between -10 and 10

# Session 1: Guided Practice (We Do – Teacher Notes)

**Materials:**

- Integer Tiles (20 positive and 20 negative tiles)
- Integer Equation Cards (1 set)

**Note:** If there is no addition or subtraction symbol between the first integer and the parentheses, then the integers should be multiplied.

$$2(-4) = 2 \times -4 \qquad -4(-5) = -4 \times -5$$

$$-3(7) = -3 \times 7 \qquad (-2)(6) = -2 \times 6$$

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use integer tiles to find the answer.

<p>1. <span style="color: red;">"3 times negative 5 is equal to 3 groups of 5 negatives"</span></p> <p><math>3(-5) = \underline{-15}</math></p>	<p>2. <span style="color: red;">"Negative 12 divided by 4 can be thought of as 4 groups of how many is negative 12?"</span></p> <p><math>-12 \div 4 = \underline{-3}</math></p> <p><span style="color: red;">4( <u>   </u> ) = -12</span></p>
<p>3. <span style="color: red;">"4 times negative 3 is equal to 4 groups of 3 negatives"</span></p> <p><math>4 \times -3 = \underline{-12}</math></p>	<p>4. <math>\overset{\text{The opposite of}}{\uparrow} \underline{-4(-3)} = \underline{12}</math></p> <p><span style="color: red;">4(3) = 12</span></p> <p><span style="color: red;">"Negative 4 times negative 3 is equal to the opposite of 4 groups of 3 negatives, which is equal to 4 groups of 3 positives"</span></p>



# Session 1: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
  
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form A

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-10 \times 4$	<b>2.</b>  $6 \times -8$
<b>3.</b>  $-9 \times -8$	<b>4.</b>  $-9 \div 3$
<b>5.</b>  $10 \div -2$	<b>6.</b>  $-10 \div -2$

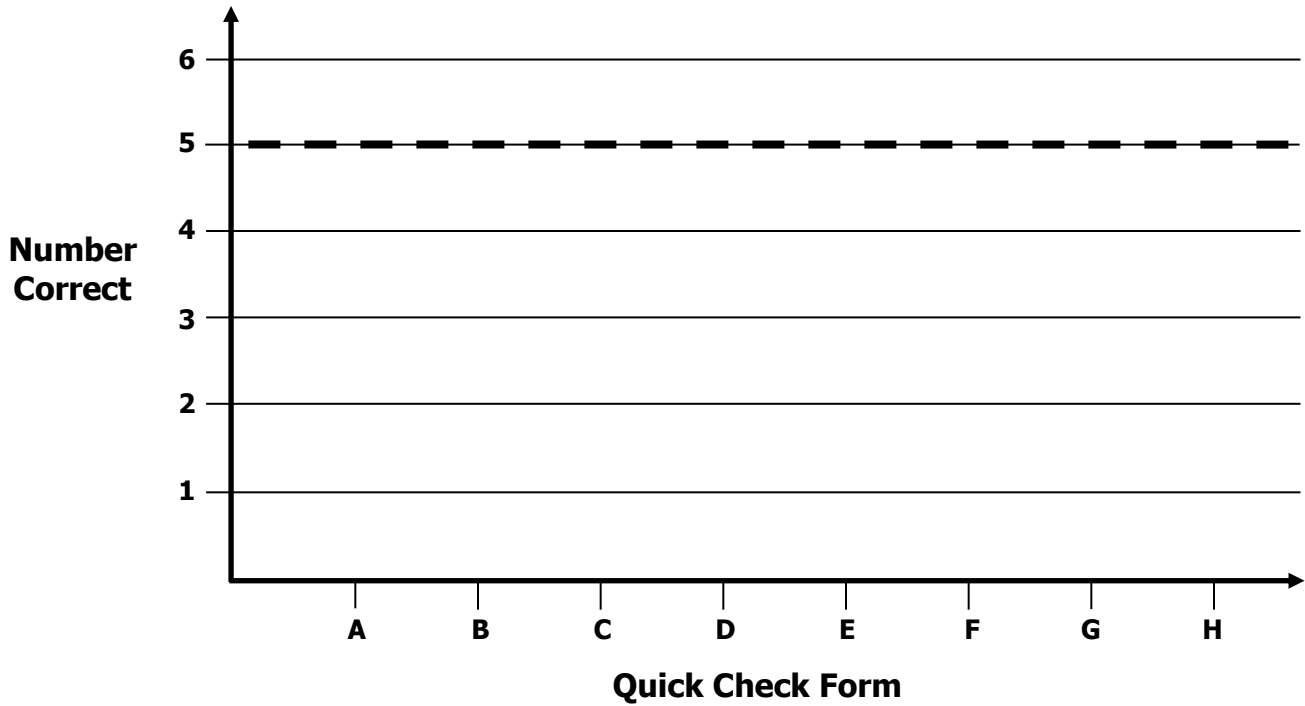


# Growth Chart

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Goal:** 5 out of 6 correct



Intervention	Date	Score
Session 1:		
Session 2:		
Session 3:		
Session 4:		
Session 5:		
Session 6:		
Session 7:		
Session 8:		



Name \_\_\_\_\_

Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 2: Guided Practice (We Do)

**Materials:**

- Integer Tiles (20 positive and 20 negative tiles)
- Integer Equation Cards (1 set – See Session 1)

**Note:** If there is no addition or subtraction symbol between the first integer and the parentheses, then the integers should be multiplied.

$$2(-4) = 2 \times -4$$

$$-3(7) = -3 \times 7$$

$$-4(-5) = -4 \times -5$$

$$(-2)(6) = -2 \times 6$$

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use integer tiles to find the answer.

<p>1.</p> $4(-5) = \underline{\quad}$	<p>2.</p> $-12 \div 3 = \underline{\quad}$
<p>3.</p> $5 \times -3 = \underline{\quad}$	<p>4.</p> $-2(-3) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 2: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to multiply or divide using integer tiles.

5. $2(-4) = \underline{\quad}$	6. $-15 \div 3 = \underline{\quad}$
7. $6 \times -3 = \underline{\quad}$	8. $-3 \times 4 = \underline{\quad}$
9. $-12 \div 2 = \underline{\quad}$	10. $-10 \div -2 = \underline{\quad}$





## Session 2: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
  
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form B

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-7 \times 3$	<b>2.</b>  $6 \times -9$
<b>3.</b>  $-5 \times -6$	<b>4.</b>  $-8 \div 4$
<b>5.</b>  $10 \div -5$	<b>6.</b>  $-12 \div -4$



## Session 3: Modeling (I Do)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

Sam's grandma keeps track of money that she loans him in a notebook called "Sam's Financial Journal". The recent balance was 0 dollars and his grandma gave him money to purchase two \$4 movies to watch at his birthday sleepover. What is the current balance in the journal?



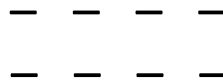
## Session 3: Modeling (Visual Support)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

Sam's grandma keeps track of money that she loans him in a notebook called "Sam's Financial Journal". The recent balance was 0 dollars and his grandma gave him money to purchase two \$4 movies to watch at his birthday sleepover. What is the current balance in the journal?

$$2 \times -4 = -8$$





# Session 3: Modeling (I Do - Teacher Notes)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

Sam’s grandma keeps track of money that she loans him in a notebook called “Sam’s Financial Journal”. The recent balance was 0 dollars and his grandma gave him money to purchase two \$4 movies to watch at his birthday sleepover. What is the current balance in the journal?

**I am going to think aloud to model solving this problem.**

**Your job is to watch, listen, think and ask questions.**

<p><b>First, it is important to know what the problem is about.</b></p> <p>The problem is about “Sam’s Financial Journal”.</p>
<p><b>Second, I need to determine what I need to find.</b></p> <p>I need to find the current balance.</p>
<p><b>Third, I need to determine what I know.</b></p> <p>I know the recent balance was 0 dollars and his grandma gave him money to purchase two \$4 movies. Also, I know money that is owed...or debt...can be represented as negative integers and money earned can be represented as positive integers.</p>
<p><b>Fourth, I need to figure out what I can try.</b></p> <p>I am going to try using a math drawing to find Sam’s current balance.</p> <p>Since I need 2 groups of 4 negative tiles to model Sam’s current debt... I will write and model the equation 2 times -4. (Write “2 x -4”.)</p> <p>Here is one group of -4 dollars. (Draw one row of 4 negative signs.)</p> <p>And here is the second group of -4 dollars. (Draw the second row of 4 negative signs below the first row.)</p> <p>I see 4...8 negative signs...that represents -8 dollars...or 8 dollars of debt to pay (Point to the 8 negative signs that make up the product.)</p>
<p><b>Last, I need to make sure that my answer makes sense.</b></p> <p>I found that Sam’s balance is 8 dollars of debt. It makes sense because I modeled the situation using a multiplication equation and drawing. Then, I modeled the product with 2 groups of 4 negative signs to show 8 dollars of debt as the current balance in the journal.</p>



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 3: Guided Practice (We Do)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use a math drawing to find the answer.

1. $3(-5) = \underline{\quad}$	2. $-12 \div 4 = \underline{\quad}$
3. $4 \times -3 = \underline{\quad}$	4. $-4(-3) = \underline{\quad}$
5. $-15 \div 3 = \underline{\quad}$	6. $-5(4) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 3: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to add and subtract integers using drawings to represent action.

7. $2(-4) = \underline{\quad}$	8. $-8 \div 2 = \underline{\quad}$
9. $6 \times -3 = \underline{\quad}$	10. $-3(5) = \underline{\quad}$
11. $-12 \div 6 = \underline{\quad}$	12. $-2(-7) = \underline{\quad}$



Name \_\_\_\_\_

Date \_\_\_\_\_

Learning Target: I will multiply and divide by integers between -10 and 10

## Session 3: Guided Practice (We Do – Teacher Notes)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use a math drawing to find the answer.

<p>1. <i>"3 times negative 5 is equal to 3 groups of 5 negatives"</i></p> $3(-5) = \underline{-15}$ <p>— — — — — — — — — — — — — — —</p>	<p>2. <i>"Negative 12 divided by 4 can be thought of as 4 groups of how many is negative 12?"</i></p> $-12 \div 4 = \underline{-3}$ <p>— — — — — — — — — — — — — — — — — — — —</p>
<p>3. <i>"4 times negative 3 is equal to 4 groups of 3 negatives"</i></p> $4 \times -3 = \underline{-12}$ <p>— — — — — — — — — — — — — — — — — — — —</p>	<p>4. <i>"Negative 4 times negative 3 is equal to the opposite of 4 groups of 3 negatives which is equal to 4 groups of 3 positives"</i></p> $\underline{-4}(-3) = \underline{12}$ <p>The opposite of <math>4(3) = \underline{\quad}</math></p> <p>+ + + + + + + + + + + +</p>
<p>5. <i>"Negative 15 divided by 3 can be thought of as 3 groups of how many is negative 15?"</i></p> $-15 \div 3 = \underline{-5}$ <p>3( <u>    </u> ) = -15?</p> <p>— — — — — — — — — — — — — — —</p>	<p>6. <i>The opposite of</i></p> $\underline{-5}(4) = \underline{-20} \quad 5(-4) = \underline{\quad}$ <p>— — — — — — — — — — — — — — — — — — — —</p> <p><i>"Negative 5 times 4 is equal to the opposite of 5 groups of 4 positives, which is equal to 5 groups of 4 negatives"</i></p>





## Session 3: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
  
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form C

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-9 \times 2$	<b>2.</b>  $5 \times -9$
<b>3.</b>  $-4 \times -8$	<b>4.</b>  $-6 \div 3$
<b>5.</b>  $18 \div -2$	<b>6.</b>  $-24 \div -8$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 4: Guided Practice (We Do)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use a math drawing to find the answer.

1. $3(-4) = \underline{\quad}$	2. $-8 \div 4 = \underline{\quad}$
3. $4 \times -5 = \underline{\quad}$	4. $-2(-3) = \underline{\quad}$
5. $-18 \div 3 = \underline{\quad}$	6. $-5(2) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 4: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to add and subtract integers using drawings to represent action.

7. $2(-6) = \underline{\quad}$	8. $-10 \div 2 = \underline{\quad}$
9. $7 \times -3 = \underline{\quad}$	10. $-3(4) = \underline{\quad}$
11. $-18 \div 6 = \underline{\quad}$	12. $-2(-9) = \underline{\quad}$



## Session 4: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form D

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-5 \times 10$	<b>2.</b>  $4 \times -7$
<b>3.</b>  $-3 \times -7$	<b>4.</b>  $-8 \div 2$
<b>5.</b>  $4 \div -2$	<b>6.</b>  $-20 \div -5$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 5: Guided Practice (We Do)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use a math drawing to find the answer.

1. $3(-6) = \underline{\quad}$	2. $-12 \div 2 = \underline{\quad}$
3. $4 \times -2 = \underline{\quad}$	4. $-4(-5) = \underline{\quad}$
5. $-15 \div 5 = \underline{\quad}$	6. $-5(3) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 5: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to add and subtract integers using drawings to represent action.

7. $2(-7) = \underline{\quad}$	8. $-12 \div 2 = \underline{\quad}$
9. $2 \times -3 = \underline{\quad}$	10. $-3(7) = \underline{\quad}$
11. $-12 \div 4 = \underline{\quad}$	12. $-2(-8) = \underline{\quad}$





## Session 5: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
  
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form E

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-10 \times 4$	<b>2.</b>  $6 \times -8$
<b>3.</b>  $-9 \times -8$	<b>4.</b>  $-9 \div 3$
<b>5.</b>  $10 \div -2$	<b>6.</b>  $-10 \div -2$



## Session 6: Modeling

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

On the Delta Math readiness screener, Sam selected the following answer choice. Is he correct? If not, why do you think he chose his answer?

Multiply:

$$-3(-5)$$

15

-15

8

-8



## Session 6: Modeling (Visual Support)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

On the Delta Math readiness screener, Sam selected the following answer choice. Is he correct? If not, why do you think he chose his answer?

Multiply:

$$\begin{array}{l} -3(-5) = 15 \\ \uparrow \\ \text{Opposite of } 3(-5) = 3(5) = 15 \end{array}$$

- 15       -15       8       -8



# Session 6: Modeling (I Do - Teacher Notes)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Readiness** for solving multi-step linear equations

On the Delta Math readiness screener, Sam selected the following answer choice. Is he correct? If not, why do you think he chose his answer?

**I am going to think aloud to model solving this problem.**

**Your job is to watch, listen, think and ask questions.**

**First, it is important to know what the problem is about.**

**This problem is about Sam answering an integer multiplication problem on a Delta Math readiness screener.**

**Second, I need to determine what I need to find.**

**I need to find if Sam chose the correct answer. And if he was not correct, I need to consider why he made the choice that he did.**

**Third, I need to determine what I know.**

**I know that Sam chose -8 as the answer to -3 times -5 and I know that the negative sign in front of the 3 means "the opposite of".**

*(Draw an arrow pointing to the first negative sign and write "Opposite of 3(-5)")*

**Fourth, I need to figure out what I can try.**

Multiply:

$$-3(-5) = 15$$

↑  
Opposite of 3(-5) = 3(5) = 15

**I am going to try using my understanding of multiplication to find the correct answer to this question.**

**Since I need to find the opposite of 3 groups of negative 5...**

**I can think of 3 groups of positive 5...which is equal to 15 positives.**

*(Write "= 3(5) = 15 and circle the answer choice "15".)*

- 15     
  -15     
  8     
  -8

**I see this is not the answer choice that Sam chose...therefore, he must have selected an incorrect answer choice.**

**I think that Sam chose his answer because he saw the two negative signs and thought 3 negatives and 5 negatives make 8 negatives...which is true if the operation was addition. But, since there is no addition symbol between the first integer and the parentheses, the operation is multiplication.**

**Last, I need to make sure that my answer makes sense.**

**I found that Sam was not correct. It makes sense because I thought about the problem as "the opposite of 3 groups of -5" to find the correct answer...15.**



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 6: Guided Practice (We Do)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use your understanding of integers to find the answer. Then, write three additional equations using the three integers.

1. $8(-5) = \underline{\quad}$	2. $-32 \div 4 = \underline{\quad}$
3. $9 \times -3 = \underline{\quad}$	4. $-6(7) = \underline{\quad}$
5. $-35 \div 7 = \underline{\quad}$	6. $-7(-8) = \underline{\quad}$
7. $6 \times -8 = \underline{\quad}$	8. $-54 \div 9 = \underline{\quad}$
9. $-63 \div 7 = \underline{\quad}$	10. $-8(9) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 6: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to multiply and divide integers.

11. $8(-4) = \underline{\quad}$	12. $-42 \div 6 = \underline{\quad}$
13. $9 \times -7 = \underline{\quad}$	14. $-6(8) = \underline{\quad}$
15. $-56 \div 7 = \underline{\quad}$	16. $-3(-8) = \underline{\quad}$
17. $9 \times -6 = \underline{\quad}$	18. $-64 \div 8 = \underline{\quad}$
19. $-54 \div 6 = \underline{\quad}$	20. $-4(9) = \underline{\quad}$

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 6: Guided Practice (We Do – Teacher Notes)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use your understanding of integers to find the answer. Then, write three additional equations using the three integers.

<p>1. <i>"8 times negative 5 is equal to 8 groups of 5 negatives"</i></p> $8(-5) = \underline{-40}$	<p>2. <i>"Negative 32 divided by 4 can be thought of as 4 groups of how many is negative 32?"</i></p> $-32 \div 4 = \underline{-8}$ $4(\underline{\quad}) = -32$
<p>3. <i>"9 times negative 3 is equal to 9 groups of 3 negatives"</i></p> $9 \times -3 = \underline{-27}$	<p>4.</p> $-6(7) = \underline{-42}$ $6(-7) = \underline{\quad}$ <p><i>"Negative 6 times 7 is equal to the opposite of 6 groups of 7, which is equal to 6 groups of negative 7"</i></p>
<p>5. <i>"Negative 35 divided by 7 can be thought of as 7 groups of how many is negative 35?"</i></p> $-35 \div 7 = \underline{-5}$ $7(\underline{\quad}) = -35$	<p>6.</p> $-7(-8) = \underline{56}$ $7(8) = \underline{\quad}$ <p><i>"Negative 7 times negative 8 is equal to the opposite of 7 groups of 8 negatives, which is equal to 7 groups of positive 8"</i></p>
<p>7. <i>"6 times negative 8 is equal to 6 groups of 8 negatives"</i></p> $6 \times -8 = \underline{-48}$	<p>8. <i>"Negative 54 divided by 9 can be thought of as 9 groups of how many is negative 54?"</i></p> $-54 \div 9 = \underline{-6}$ $9(\underline{\quad}) = -54$
<p>9. <i>"Negative 63 divided by 7 can be thought of as 7 groups of how many is negative 63?"</i></p> $-63 \div 7 = \underline{-9}$ $7(\underline{\quad}) = -63$	<p>10.</p> $-8(9) = \underline{-72}$ $8(-9) = \underline{\quad}$ <p><i>"Negative 8 times 9 is equal to the opposite of 8 groups of positive 9, which is equal to 8 groups of negative 9"</i></p>





## Session 6: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form F

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-7 \times 3$	<b>2.</b>  $6 \times -9$
<b>3.</b>  $-5 \times -6$	<b>4.</b>  $-8 \div 4$
<b>5.</b>  $10 \div -5$	<b>6.</b>  $-12 \div -4$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 7: Guided Practice (We Do)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use your understanding of integers to find the answer. Then, write three additional equations using the three integers.

1. $8(-6) = \underline{\quad}$	2. $-36 \div 4 = \underline{\quad}$
3. $9 \times -5 = \underline{\quad}$	4. $-6(8) = \underline{\quad}$
5. $-42 \div 7 = \underline{\quad}$	6. $-7(-9) = \underline{\quad}$
7. $7 \times -8 = \underline{\quad}$	8. $-54 \div 6 = \underline{\quad}$
9. $-28 \div 7 = \underline{\quad}$	10. $-8(6) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 7: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to multiply and divide integers.

11. $9(-4) = \underline{\quad}$	12. $-48 \div 6 = \underline{\quad}$
13. $8 \times -7 = \underline{\quad}$	14. $-6(7) = \underline{\quad}$
15. $-54 \div 9 = \underline{\quad}$	16. $-6(-8) = \underline{\quad}$
17. $9 \times -7 = \underline{\quad}$	18. $-81 \div 9 = \underline{\quad}$
19. $-54 \div 9 = \underline{\quad}$	20. $-9(6) = \underline{\quad}$



## Session 7: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form G

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

**1.**

$$-9 \times 2$$

**2.**

$$5 \times -9$$

**3.**

$$-4 \times -8$$

**4.**

$$-6 \div 3$$

**5.**

$$18 \div -2$$

**6.**

$$-24 \div -8$$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 8: Guided Practice (We Do)

**We Do Together:** (Teacher Actions)

- Say what you are trying to find and use your understanding of integers to find the answer. Then, write three additional equations using the three integers.

1. $7(-5) = \underline{\quad}$	2. $-28 \div 4 = \underline{\quad}$
3. $8 \times -3 = \underline{\quad}$	4. $-9(7) = \underline{\quad}$
5. $-35 \div 5 = \underline{\quad}$	6. $-6(-8) = \underline{\quad}$
7. $6 \times -9 = \underline{\quad}$	8. $-56 \div 8 = \underline{\quad}$
9. $-56 \div 7 = \underline{\quad}$	10. $-8(6) = \underline{\quad}$



Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10

## Session 8: Guided Practice (We Do - Continued)

**You Do Together:** (As a class, or in small groups)

- Students take turns leading to multiply and divide integers.

11. $8(-3) = \underline{\quad}$	12. $-42 \div 7 = \underline{\quad}$
13. $9 \times -6 = \underline{\quad}$	14. $-6(8) = \underline{\quad}$
15. $-56 \div 8 = \underline{\quad}$	16. $-4(-7) = \underline{\quad}$
17. $9 \times -3 = \underline{\quad}$	18. $-49 \div 7 = \underline{\quad}$
19. $-54 \div 6 = \underline{\quad}$	20. $-4(7) = \underline{\quad}$





## Session 8: Self-Reflection

**Learning Target:** I will multiply and divide by integers between -10 and 10

Briefly discuss student responses

- What did I learn today about multiplying and dividing by integers between -10 and 10?
  
- How confident do I feel about multiplying and dividing by integers between -10 and 10? (*Thumbs up, down, or sideways*)



# Quick Check - Form H

Name \_\_\_\_\_ Date \_\_\_\_\_

**Learning Target:** I will multiply and divide by integers between -10 and 10.

**Directions:** Write the answer to each problem. (Work time: 2 minutes)

<b>1.</b>  $-5 \times 10$	<b>2.</b>  $4 \times -7$
<b>3.</b>  $-3 \times -7$	<b>4.</b>  $-8 \div 2$
<b>5.</b>  $4 \div -2$	<b>6.</b>  $-20 \div -5$



# Independent Practice (You Do)

**Learning Target:** I will multiply and divide by integers between -10 and 10

**Title of Game:** “Multiply and Divide Integer: Match-ups”

**Number of Players:** 2

**Objective:** To be the first player to match all 5 cards.

**Materials:**

- Multiply and Divide Integers: **Problem Cards** (1 set)
- Multiply and Divide Integers: **Answer Cards** (1 set)
- Making Meaning: Match-ups: Recording sheet (1 per student - Optional)

**Directions:**

- Place a set of **Problem Cards** face-down in a row.
- Place a set of **Answer Cards** face-up underneath the row, 5 for each player.
- Player 1 turns over a **Problem Card** to see if it matches one of their **Answer cards**.
  - If there is an equivalent expression, say the addition expression, describe how to get the answer and the answer. Then, pick up the card and place it below your card.
  - If there is not an equivalent expression, then say “Not Equivalent” and turn the card back over.
- Player 2 turns over a **Problem Card** to see if it matches one of their **Answer cards**.
  - If there is an equivalent expression, say the addition expression, describe how to get the answer and the answer. Then, pick up the card and place it below your card.
  - If there is not an equivalent expression, then say “Not Equal” and turn the card back over.
- Repeat
- The winner is the first player to match all 5 cards.

**Math Talk:**

*“I have an equivalent expression... 2 groups of 3 negatives is equal to 6 negatives.”*



# Multiply and Divide Integers: Problem Cards (Set A)

**Storage Suggestions:** Copy the **Equation (Set A)** cards and **Answer (Set A)** cards in two different colors.  
Store 1 set of each in a sealable bag for each pair of students.

$$5(-6) = \underline{\quad}$$

Set A

$$-5(-6) = \underline{\quad}$$

Set A

$$-7(8) = \underline{\quad}$$

Set A

$$-7 \times -8 = \underline{\quad}$$

Set A

$$-6(-8) = \underline{\quad}$$

Set A

$$6(-8) = \underline{\quad}$$

Set A

$$-28 \div -7 = \underline{\quad}$$

Set A

$$-28 \div 7 = \underline{\quad}$$

Set A

$$56 \div -7 = \underline{\quad}$$

Set A

$$-56 \div -7 = \underline{\quad}$$

Set A



# Multiply and Divide Integers: Answer Cards (Set A)

**Storage Suggestions:** Copy the **Equation (Set A)** cards and **Answer (Set A)** cards in two different colors.  
Store 1 set of each in a sealable bag for each pair of students.

$-30$ <i>Set A</i>	$30$ <i>Set A</i>
$-56$ <i>Set A</i>	$56$ <i>Set A</i>
$48$ <i>Set A</i>	$-48$ <i>Set A</i>
$4$ <i>Set A</i>	$-4$ <i>Set A</i>
$-8$ <i>Set A</i>	$8$ <i>Set A</i>



# Multiply and Divide Integers: Problem Cards (Set B)

**Storage Suggestions:** Copy the **Equation (Set B)** cards and **Answer (Set B)** cards in two different colors.  
Store 1 set of each in a sealable bag for each pair of students.

$$6(-7) = \underline{\quad}$$

Set B

$$-6(-7) = \underline{\quad}$$

Set B

$$-8(9) = \underline{\quad}$$

Set B

$$-8 \times -9 = \underline{\quad}$$

Set B

$$-7(-9) = \underline{\quad}$$

Set B

$$7(-9) = \underline{\quad}$$

Set B

$$-27 \div -3 = \underline{\quad}$$

Set B

$$-27 \div 3 = \underline{\quad}$$

Set B

$$54 \div -9 = \underline{\quad}$$

Set B

$$-54 \div -9 = \underline{\quad}$$

Set B



# Multiply and Divide Integers: Answer Cards (Set B)

**Storage Suggestions:** Copy the **Equation (Set B)** cards and **Answer (Set B)** cards in two different colors.  
Store 1 set of each in a sealable bag for each pair of students.

-42 <i>Set B</i>	42 <i>Set B</i>
-72 <i>Set B</i>	72 <i>Set B</i>
63 <i>Set B</i>	-63 <i>Set B</i>
9 <i>Set B</i>	-9 <i>Set B</i>
-6 <i>Set B</i>	6 <i>Set B</i>



# Questions for Solving Word Problems

Q<sub>1</sub>

*What is the problem about?*

Q<sub>2</sub>

*What do I need to find?*

Q<sub>3</sub>

*What do I know?*

Q<sub>4</sub>

*What can I try?*

Q<sub>5</sub>

*Does my answer make sense?*





# Steps for Solving Word Problems

Q<sub>1</sub>. *What is the problem about?*

Q<sub>2</sub>. *What do I need to find?*

Q<sub>3</sub>. *What do I know?*

Q<sub>4</sub>. *What can I try?*

Q<sub>5</sub>. *Does my answer make sense?*